

ecl-es-halt^{0,22}

ecl-es-halt($es;x$)
 $\equiv_{\text{def}} \text{ecl_ind}(x;k,\text{test}.\lambda n,e_1,e_2. \text{ if } n=20 \rightarrow$
 $$e_2 =$
 $\text{first } e \geq e_1.\text{kind}(e) = k \ \& \ \text{test}((\text{state when } e), \text{val}(e))$
 $\text{else False fi;} a,b,ha,hb.\lambda n,e_1,e_2. \text{ if } n=20 \rightarrow \text{False}$
 $\text{else } ha(n,e_1,e_2) \text{ fi}$$
 $\vee \exists e \in (e_1, e_2]. ha(0, e_1, \text{pred}(e)) \ \& \ hb(n, e, e_2); a, b, ha, hb.\lambda n, e_1, e_2.$
 $\text{if } n=20 \rightarrow ha(0, e_1, e_2) \ \& \ \exists e \in [e_1, e_2]. hb(0, e_1, e) \vee hb(0, e_1, e_2) \ \& \ \exists e \in [e_1, e_2]. ha(0, e_1, e)$
 $\text{else } ha(n, e_1, e_2)$
 $\quad \& \forall m \in 0.\text{ecl-ex}(b). \text{if } n \leq 2m \rightarrow \forall e \in [e_1, e_2]. \neg hb(m, e_1, e) \text{ else } \forall e \in [e_1, e_2]. \neg hb(m, e_1, e) \text{ fi}$
 $\quad \vee hb(n, e_1, e_2)$
 $\quad \& \forall m \in 0.\text{ecl-ex}(a).$
 $\quad \quad \text{if } n \leq 2m \rightarrow \forall e \in [e_1, e_2]. \neg ha(m, e_1, e)$
 $\quad \quad \text{else } \forall e \in [e_1, e_2]. \neg ha(m, e_1, e) \text{ fi;} a, b, ha, hb.\lambda n, e_1, e_2. ha(n, e_1, e_2)$
 $\quad \& \forall m \in 0.\text{ecl-ex}(b). \text{if } n \leq 2m \rightarrow \forall e \in [e_1, e_2]. \neg hb(m, e_1, e) \text{ else } \forall e \in [e_1, e_2]. \neg hb(m, e_1, e) \text{ fi}$
 $\quad \vee hb(n, e_1, e_2)$
 $\quad \& \forall m \in 0.\text{ecl-ex}(a).$
 $\quad \quad \text{if } n \leq 2m \rightarrow \forall e \in [e_1, e_2]. \neg ha(m, e_1, e) \text{ else } \forall e \in [e_1, e_2]. \neg ha(m, e_1, e) \text{ fi;} a, ha.\lambda n, e_1, e_2.$
 $\text{if } n=20 \rightarrow \text{False}$
 $\text{else } [e_1; e_2] \sim ([x, y]. ha(0, x, y)) * [x, y]. ha(n, x, y) \text{ fi;} a, m, ha.ha; a, m, ha.\lambda n, e_1, e_2.$
 $\text{if } n=20 \rightarrow \text{False} \text{ else } ha(n, e_1, e_2) \text{ fi}$
 $\vee \text{if } n=20 \rightarrow ha(0, e_1, e_2) \text{ else False fi;} a, l, ha.\lambda n, e_1, e_2. ha(n, e_1, e_2) \ \& \ \neg(n \in l)$
 $\vee \text{if } n=20 \rightarrow (\exists m \in l. ha(m, e_1, e_2)) \text{ else False fi}$

clarification:

ecl-es-halt($es;x$)
 $\equiv_{\text{def}} \text{ecl_ind}(x;k,\text{test}.\lambda n,e_1,e_2. \text{ if } n=20 \rightarrow$
 $\text{es-first-since}(es; e.\text{es-kind}(es; e) = k \in \text{Knd})$
 $\& \text{test}(\text{es-state-when}(es; e), \text{es-val}(es; e)); e_1; e_2)$
 $\text{else False fi;} a, b, ha, hb.\lambda n, e_1, e_2. \text{ if } n=20 \rightarrow \text{False}$
 $\text{else } ha(n, e_1, e_2) \text{ fi}$

 $\vee \text{existse-between3}(es; e_1; e_2; e. ha(0, e_1, \text{es-pred}(es; e))$
 $\& hb(n, e, e_2)); a, b, ha, hb.\lambda n, e_1, e_2.$
 $\text{if } n=20 \rightarrow$
 $ha(0, e_1, e_2) \ \& \ \text{existse-between2}(es; e_1; e_2; e. hb(0, e_1, e))$
 $\vee hb(0, e_1, e_2) \ \& \ \text{existse-between2}(es; e_1; e_2; e. ha(0, e_1, e))$
 $\text{else } ha(n, e_1, e_2)$
 $\quad \& \forall m \in 0.\text{ecl-ex}(b).$
 $\quad \quad \text{if } n \leq 2m \rightarrow \text{alle-between1}(es; e_1; e_2; e. \neg hb(m, e_1, e))$
 $\quad \quad \text{else alle-between2}(es; e_1; e_2; e. \neg hb(m, e_1, e)) \text{ fi}$
 $\vee hb(n, e_1, e_2)$

$\& \forall m \in 0.\text{ecl-ex}(a).$
 if $n \leq_2 m \rightarrow \text{alle-between1}(es; e_1; e_2; e. \neg ha(m, e_1, e))$
 else $\text{alle-between2}(es; e_1; e_2; e. \neg ha(m, e_1, e)) \text{ fi fi}; a, b, ha, hb. \lambda n, e_1, e_2. ha(n, e_1, e_2)$
 $\& \forall m \in 0.\text{ecl-ex}(b).$
 if $n \leq_2 m \rightarrow \text{alle-between1}(es; e_1; e_2; e. \neg hb(m, e_1, e))$
 else $\text{alle-between2}(es; e_1; e_2; e. \neg hb(m, e_1, e)) \text{ fi}$
 $\vee hb(n, e_1, e_2)$
 $\& \forall m \in 0.\text{ecl-ex}(a).$
 if $n \leq_2 m \rightarrow \text{alle-between1}(es; e_1; e_2; e. \neg ha(m, e_1, e))$
 else $\text{alle-between2}(es; e_1; e_2; e. \neg ha(m, e_1, e)) \text{ fi}; a, ha. \lambda n, e_1, e_2.$
 if $n =_2 0 \rightarrow \text{False}$
 else $\text{es-pstar-q}(es; x, y. ha(0, x, y); x, y. ha(n, x, y); e_1, e_2) \text{ fi}; a, m, ha. ha; a, m, ha. \lambda n, e_1, e_2.$
 if $n =_2 0 \rightarrow \text{False}$ else $ha(n, e_1, e_2) \text{ fi}$
 \vee if $n =_2 m \rightarrow ha(0, e_1, e_2)$ else $\text{False} \text{ fi}; a, l, ha. \lambda n, e_1, e_2. ha(n, e_1, e_2) \& \neg(n \in l \in \mathbb{N})$
 \vee if $n =_2 0 \rightarrow \text{l_exists}(l; \mathbb{N}; m. ha(m, e_1, e_2))$ else $\text{False} \text{ fi}$